



## Preface

### **Content**

Interactive design aids for timber elements in accordance to BS EN 1995

### **Guidelines of use**

After installing a free trial or demo version the interactive templates will be available free of charge. The only requirement is a registration at [www.VCmaster.com](http://www.VCmaster.com).

The examples provided have been created using VCmaster. All annotated and illustrated design aids can be used as a basis to create own templates. In order to do this a full version of VCmaster is necessary.

All templates are linked to various databases by TAB()- or SEL() functions. For instructional purposes these links are displayed in this document, but can also be hidden when printing.

### **What is VCmaster?**

VCmaster is a software application for technical documentation specifically designed for engineers. The unique software concept integrates all structural design and CAD software. Universal interfaces guarantee data transfer, so that the output of all programs can be transposed.

Beside its functions for documentation, VCmaster offers an intuitive concept enabling engineers to carry out calculations. The input of mathematic formulas can be executed in natural notation directly in the document itself. The software significantly supports the reuse of structural calculations and documents. VCmaster simplifies modifications and adjustments and automates standard tasks. Collaboration with work-groups or with other offices and clients is uncomplicated as well. As a result, processing time and costs can be considerably reduced.

### **System Requirements**

VCmaster 2016 or newer

### **Development and Copyrights**

Developed in Germany  
VCmaster is a registered trademark  
© Veit Christoph GmbH 1995-2016  
[www.VCmaster.com](http://www.VCmaster.com)



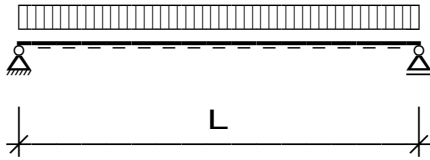
## Contents

<b>Preface</b>	1
<b>Contents</b>	2
<b>Chapter 1: Beams</b>	3
Check of a timber beam at the bending ULS	3
Check of a beam for deflection SLS	4
Check of a timber beam at the bending ULS	6
Check of a residential floor against the vibration criterion	7
Design of a timber joist at ULS and SLS	8
<b>Chapter 2: Columns</b>	11
Axial load capacity of a timber post	11
Axial load capacity of a timber post	12
<b>Chapter 3: Supports</b>	14
Compression perpendicular to the grain at end bearing	14
Compression perpendicular to the grain at internal bearing	15
Shear capacity at a support	16
Shear capacity at a support notched at the bottom	17
Shear capacity at a support notched at the top	18



## Chapter 1: Beams

### Check of a timber beam at the bending ULS



#### Data given:

Beam span L =	4.00 m
Width b =	100.0 mm
Depth h =	150.0 mm

#### Loading

Dead load $G_k =$	2.00 kN
Imposed load $Q_k =$	3.50 kN

$$\text{Ultimate load } F_d = 1.35 * G_k + 1.50 * Q_k = 7.95 \text{ kN}$$

$$\text{Moment } M_d = \frac{F_d * L}{8} = \frac{7.95 * 4.00}{8} = 3.98 \text{ kNm}$$

#### Material properties:

Timber T	=	Softwood
Strength class $C_T$	=	C24
Service class $C_S$	=	2
Duration class $C_D$	=	medium-term

$$\text{Partial factor } \gamma_M = 1.30$$

$$f_{m,k} = 24.00 \text{ N/mm}^2$$

$$k_{mod} = 0.80$$

#### Ultimate moment of resistance

$$\text{Depth factor } k_h = \text{MAX}( 1.0 ; \text{MIN}( (150/h)^{0.2} ; 1.3 ) ) = 1.00$$

$$\text{Bending strength } f_{m,d} = k_{mod} * k_h * \frac{f_{m,k}}{\gamma_M} = 0.80 * 1.00 * \frac{24.00}{1.30} = 14.77 \text{ N/mm}^2$$

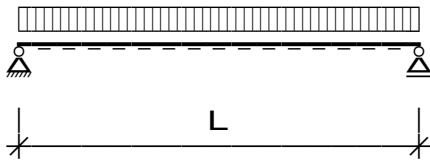
$$\text{Modulus } W_{yy} = \frac{b * h^2}{6} = \frac{100.0 * 150.0^2}{6} = 375000.0 \text{ mm}^3$$

$$M_{ult} = f_{m,d} * W_{yy} = 14770 * 0.000375 = 5.54 \text{ kNm}$$

$$\frac{M_d}{M_{ult}} = \frac{3.98}{5.54} = 0.72 \leq 1$$



### Check of a beam for deflection SLS



#### Data given:

Span L =	4.00 m
Width b =	100.0 mm
Depth h =	150.0 mm

#### Loading

Dead load $G_k =$	2.0 kN
Imposed load $Q_k =$	3.5 kN

#### Material and stiffness properties

Timber T	=	Softwood
Strength class $C_T$	=	C24
E	=	11000.00 N/mm <sup>2</sup>

A =	$b * h$	=	$15.00 * 10^3 \text{ mm}^2$
I =	$\frac{b * h^3}{12}$	=	$28.13 * 10^6 \text{ mm}^4$

#### Instantaneous Deflection

For dead load:

$$M = \frac{G_k * L}{8} = 1.00 \text{ kNm}$$

$$w_{inst,G} = \frac{5 * G_k * L^3}{384 * E * I} + \frac{19.2 * M * 10^6}{E * A} = 5.50 \text{ mm}$$

For imposed load:

$$M = \frac{Q_k * L}{8} = 1.75 \text{ kNm}$$

$$w_{inst,Q} = \frac{5 * Q_k * L^3}{384 * E * I} + \frac{19.2 * M * 10^6}{E * A} = 9.63 \text{ mm}$$

Total instantaneous deflection:

$$w_{inst} = w_{inst,G} + w_{inst,Q} = 5.50 + 9.63 = 15.13 \text{ mm}$$



### Final deflection

Category = B: office areas

$\psi_2$  = 0.30

Service class  $C_S$  = 2

$k_{def}$  = 0.80

$w_{fin,G} = w_{inst,G} * (1 + k_{def}) = 5.50 * (1 + 0.80) = 9.90 \text{ mm}$

$w_{fin,Q} = w_{inst,Q} * (1 + \psi_2 * k_{def}) = 9.63 * (1 + 0.30 * 0.80) = 11.94 \text{ mm}$

Total final deflection

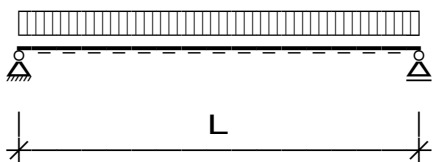
$w_{fin} = w_{fin,G} + w_{fin,Q} = 9.90 + 11.94 = 21.8 \text{ mm}$

$w_{max} = \frac{L}{150} = \frac{4000}{150} = 26.7 \text{ mm}$

$\frac{w_{fin}}{w_{max}} = \frac{21.8}{26.7} = 0.82 \leq 1$



### Check of a timber beam at the bending ULS



#### Data given:

Beam span L =	4.00 m
Width b =	100.0 mm
Depth h =	150.0 mm

#### Loading

Dead load $G_k =$	2.00 kN
Imposed load $Q_k =$	3.50 kN

$$\text{Ultimate load } F_d = 1.35 * G_k + 1.50 * Q_k = 7.95 \text{ kN}$$

$$\text{Moment } M_d = \frac{F_d * L}{8} = \frac{7.95 * 4.00}{8} = 3.98 \text{ kNm}$$

#### Material properties:

Timber T	=	Softwood
Strength class $C_T$	=	C24
Service class $C_S$	=	1
Duration class $C_D$	=	short-term
Partial factor $\gamma_M =$		1.30
$f_{m,k}$	=	24.00 N/mm <sup>2</sup>
$k_{mod}$	=	0.90

#### Maximum depth-to-breadth ratio to avoid lateral torsional buckling (LTB)

$$\text{Limiting height/breadth ratio} = 5:1$$

$$\begin{aligned} \text{Height/breadth ratio} &= h/b = 1.5 : 1 \\ \text{Maximum height} &= b * \text{factor} = 500.0 > h \end{aligned}$$

The beam is not subject to lateral torsional buckling

#### Ultimate moment of resistance

$$\text{Depth factor } k_h = \text{MAX}( 1.0 ; \text{MIN}( (150/h)^{0.2} ; 1.3 ) ) = 1.00$$

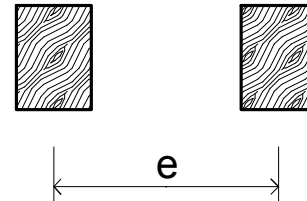
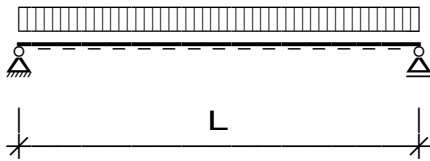
$$\text{Bending strength } f_{m,d} = k_{mod} * k_h * \frac{f_{m,k}}{\gamma_M} = 0.90 * 1.00 * \frac{24.00}{1.30} = 16.62 \text{ N/mm}^2$$

$$\text{Modulus } W_{yy} = \frac{b * h^2}{6} = \frac{100.0 * 150.0^2}{6} = 375000.0 \text{ mm}^3$$

$$M_{ult} = f_{m,d} * W_{yy} = 16620 * 0.000375 = 6.23 \text{ kNm}$$



### Check of a residential floor against the vibration criterion



#### Data given:

Span L =	4.00 m
Joist spacing e =	400.0 mm
Width b =	100.0 mm
Depth h =	150.0 mm

#### Loading

Timber T	=	Softwood
Strength class C <sub>T</sub>	=	C24
p <sub>mean</sub>	=	420.00 kg/m <sup>2</sup>

Mass of joist:	$b \cdot h \cdot \rho_{\text{mean}} / e = 0.1 \cdot 0.15 \cdot 420.00 / 0.4$	=	15.8 kg/m <sup>2</sup>
Chipboard:			15.0 kg/m <sup>2</sup>
Plasterboard:			20.0 kg/m <sup>2</sup>

**Total mass on floor m = 50.8 kg/m<sup>2</sup>**

#### EI value of one metre of floor

On joist I<sub>1</sub>:  $\frac{b \cdot h^3}{12} = \frac{100.0 \cdot 150.0^3}{12} = 28.1 \cdot 10^6 \text{ mm}^4$

I value of metre with I =  $\frac{I_1}{e} = \frac{28100000}{0.4} = 70.3 \cdot 10^6 \text{ mm}^4$

Modulus of elasticity E = 11000.0 N/mm<sup>2</sup>

EI =  $I \cdot E / 10^6 = 0.77 \cdot 10^6 \text{ Nm}^2/\text{m}$

#### First fundamental frequency f<sub>1</sub>

$f_1 = \frac{\pi}{2 \cdot L^2} \cdot \sqrt{\frac{EI}{m}} = \frac{3.14159}{2 \cdot 4.00^2} \cdot \sqrt{\frac{770000}{50.8}} = 12.09 \text{ Hz}$

f<sub>1</sub> is more than 8 Hz, so a special investigation is not required

#### Deflection under 1-kN point load

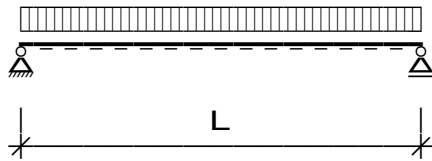
$w = \frac{399 \cdot L^3}{48 \cdot E \cdot I_1} = \frac{399 \cdot 4000^3}{48 \cdot 11000.0 \cdot 28100000} = 1.72 \text{ mm}$

$w_{\text{lim}} = \text{MIN}\left(\frac{16500}{L^{1.1}}; 1.80\right) = 1.80 \text{ mm}$

$\frac{w}{w_{\text{lim}}} = \frac{1.72}{1.80} = 0.96 \leq 1$



### Design of a timber joist at ULS and SLS



#### Data given:

Span L =	4.00 m
Joist spacing e =	600.0 mm
Width b =	100.0 mm
Depth h =	200.0 mm

#### Load on one joist

Asphalt:	$0.45 * e * L = 0.45 * 0.6 * 4.00$	=	1.08 kN
Insulation:	$0.10 * e * L = 0.10 * 0.6 * 4.00$	=	0.24 kN
Roof decking boards:	$0.30 * e * L = 0.30 * 0.6 * 4.00$	=	0.72 kN
Timber firrings:	$0.01 * e * L = 0.01 * 0.6 * 4.00$	=	0.02 kN
Suspended tile ceiling:	$0.15 * e * L = 0.15 * 0.6 * 4.00$	=	0.36 kN
Assumed self weight:	$0.10 * e * L = 0.10 * 0.6 * 4.00$	=	0.24 kN

$$G_k = \underline{\underline{2.66 \text{ kN}}}$$

$$\text{Snow load } Q_k: \quad 0.60 * e * L = 0.60 * 0.6 * 4.00 \quad = \quad 1.44 \text{ kN}$$

$$F_{SLS} = \quad G_k + Q_k = 2.66 + 1.44 \quad = \quad 4.10 \text{ kN}$$

$$F_{ULS} = \quad 1.35 * G_k + 1.50 * Q_k = 1.35 * 2.66 + 1.50 * 1.44 \quad = \quad 5.75 \text{ kN}$$

#### Timber properties and parameters

Timber T	=	Softwood
Strength class $C_T$	=	C24
Service class $C_S$	=	1
Duration class $C_D$	=	short-term
Partial factor $\gamma_M$	=	1.30
$f_{m,k}$	=	24.00 N/mm <sup>2</sup>
$f_{c,90,k}$	=	2.50 N/mm <sup>2</sup>
$f_{v,k}$	=	2.50 N/mm <sup>2</sup>
E	=	11000.00 N/mm <sup>2</sup>
$k_{sys}$	=	1.10
$k_{mod}$	=	0.90
$k_h$	=	1.00
$k_{def}$	=	0.60





### Bending ULS

$$M_d = \frac{F_{ULS} * L}{8} = \frac{5.75 * 4.00}{8} = 2.88 \text{ kNm}$$

$$\text{Bending strength } f_{m,d} = \frac{k_{sys} * k_{mod} * k_h * f_{m,k}}{\gamma_M} = \frac{1.10 * 0.90 * 1.00 * 24.00}{1.30} = 18.28 \text{ N/mm}^2$$

$$\text{Modulus } W_{yy} = \frac{b * h^2}{6} = \frac{100.0 * 200.0^2}{6} = 666666.7 \text{ mm}^3$$

$$M_{ult} = f_{m,d} * W_{yy} = 18280 * 0.0006666667 = 12.19 \text{ kNm}$$

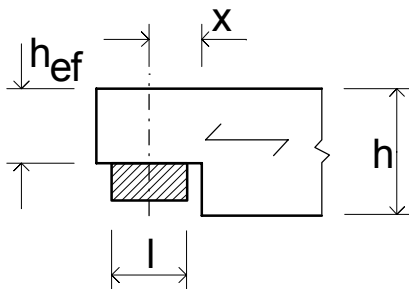
$$\frac{M_d}{M_{ult}} = \frac{2.88}{12.19} = 0.24 \leq 1$$

### Maximum depth-to-breadth ratio to avoid lateral torsional buckling (LTB)

$$\begin{aligned} \text{Limiting height/breadth ratio} &= 5:1 \\ \text{Height/breadth ratio} = h/b &= 2.0 : 1 \\ \text{Maximum height} = b * \text{factor} &= 500.0 > h \end{aligned}$$

The beam is not subject to lateral torsional buckling

### Shear ULS



### Data given

$$\begin{aligned} \text{Depth } h_{ef} &= 100.0 \text{ mm} \\ \text{Distance } x &= 50.0 \text{ mm} \\ \text{Support } l &= 100.0 \text{ mm} \end{aligned}$$

### Shear capacity

$$V = \frac{F_{ULS}}{2} = \frac{5.75}{2} = 2.88 \text{ kN}$$

$$\alpha = \frac{h_{ef}}{h} = \frac{100.0}{200.0} = 0.50$$

$$k_v = \text{MIN}\left(\frac{5}{\sqrt{h} * \left(\sqrt{\alpha * (1 - \alpha)} + 0.8 * \frac{x}{h} * \sqrt{\frac{1 - \alpha^2}{\alpha}}\right)}; 1\right) = 0.462$$

$$\text{Shear stress } \tau_d = \frac{1.5 * V}{b * h_{ef}} = \frac{1.5 * 2880}{100.0 * 100.0} = 0.43 \text{ N/mm}^2$$

$$\text{Shear strength } f_{v,d} = \frac{k_{sys} * k_{mod} * k_v * f_{v,k}}{\gamma_M} = \frac{1.10 * 0.90 * 0.462 * 2.50}{1.30} = 0.88 \text{ N/mm}^2$$

$$\frac{\tau_d}{f_{v,d}} = \frac{0.43}{0.88} = 0.49 \leq 1$$



### Bearing ULS

$$\sigma_{c,90,d} = \frac{V}{b \cdot l} = \frac{2880}{100.0 \cdot 100.0} = 0.29 \text{ N/mm}^2$$

$$k_{c,90} = \text{MAX}(1; \text{MIN}\left(\left(2.38 - \frac{l}{250}\right) \cdot \left(1 + \frac{h}{12 \cdot l}\right); 4\right)) = 2.31$$

$$f_{c,90,d} = \frac{k_{c,90} \cdot k_{\text{sys}} \cdot k_{\text{mod}} \cdot f_{c,90,k}}{\gamma_M} = \frac{2.31 \cdot 1.10 \cdot 0.90 \cdot 2.50}{1.30} = 4.40 \text{ N/mm}^2$$

$$\frac{\sigma_{c,90,d}}{f_{c,90,d}} = \frac{0.29}{4.40} = 0.07 \leq 1$$

### Deflection SLS

$$E = 11000.00 \text{ N/mm}^2$$

$$A = b \cdot h = 20.00 \cdot 10^3 \text{ mm}^2$$

$$I = \frac{b \cdot h^3}{12} = 66.67 \cdot 10^6 \text{ mm}^4$$

Instantaneous deflection for dead load:

$$M = \frac{G_k \cdot L}{8} = 1.33 \text{ kNm}$$

$$w_{\text{inst},G} = \frac{5 \cdot G_k \cdot L^3}{384 \cdot E \cdot I} + \frac{19.2 \cdot M \cdot 10^6}{E \cdot A} = 3.14 \text{ mm}$$

Instantaneous deflection for imposed load:

$$M = \frac{Q_k \cdot L}{8} = 0.72 \text{ kNm}$$

$$w_{\text{inst},Q} = \frac{5 \cdot Q_k \cdot L^3}{384 \cdot E \cdot I} + \frac{19.2 \cdot M \cdot 10^6}{E \cdot A} = 1.70 \text{ mm}$$

Total instantaneous deflection:

$$w_{\text{inst}} = w_{\text{inst},G} + w_{\text{inst},Q} = 3.14 + 1.70 = 4.84 \text{ mm}$$

Final deflection

Catagory = Snow

$$\psi_2 = 0.00$$

$$k_{\text{def}} = 0.60$$

$$w_{\text{fin},G} = w_{\text{inst},G} \cdot (1 + k_{\text{def}}) = 3.14 \cdot (1 + 0.60) = 5.02 \text{ mm}$$

$$w_{\text{fin},Q} = w_{\text{inst},Q} \cdot (1 + \psi_2 \cdot k_{\text{def}}) = 1.70 \cdot (1 + 0.00 \cdot 0.60) = 1.70 \text{ mm}$$

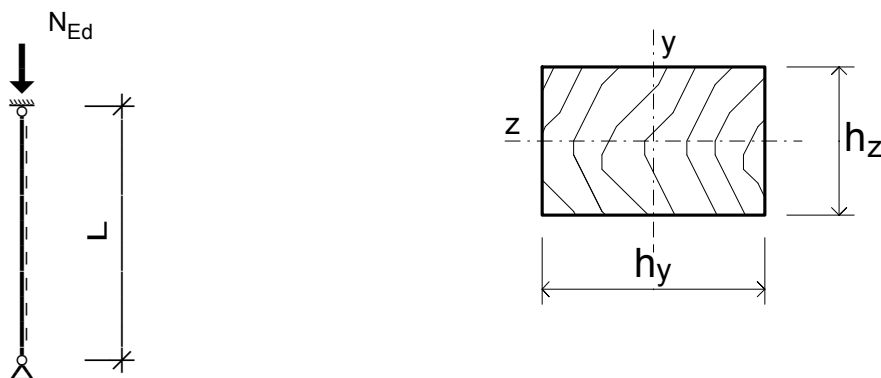
$$w_{\text{fin}} = w_{\text{fin},G} + w_{\text{fin},Q} = 5.02 + 1.70 = 6.7 \text{ mm}$$

$$w_{\text{max}} = \frac{L}{150} = \frac{4000}{150} = 26.7 \text{ mm}$$

$$\frac{w_{\text{fin}}}{w_{\text{max}}} = \frac{6.7}{26.7} = 0.25 \leq 1$$

## Chapter 2: Columns

### Axial load capacity of a timber post



#### Data given

Clear height $L =$	3.50 m
Depth $h_z =$	100.0 mm
Depth $h_y =$	150.0 mm

#### Timber properties and parameters

Timber $T$	=	Softwood
Strength class $C_T$	=	C24
Service class $C_S$	=	2
Duration class $C_D$	=	medium-term
$E_{0,0,05}$	=	7400.00 N/mm <sup>2</sup>
$f_{c,0,k}$	=	21.00 N/mm <sup>2</sup>
$k_{mod}$	=	0.80
Design compressive strength of timber:		
$f_{c,0,d} =$	$k_{mod} * f_{c,0,k} / \gamma_M = 0.80 * 21.00 / 1.30$	= 12.92 N/mm <sup>2</sup>

#### Calculations for buckling

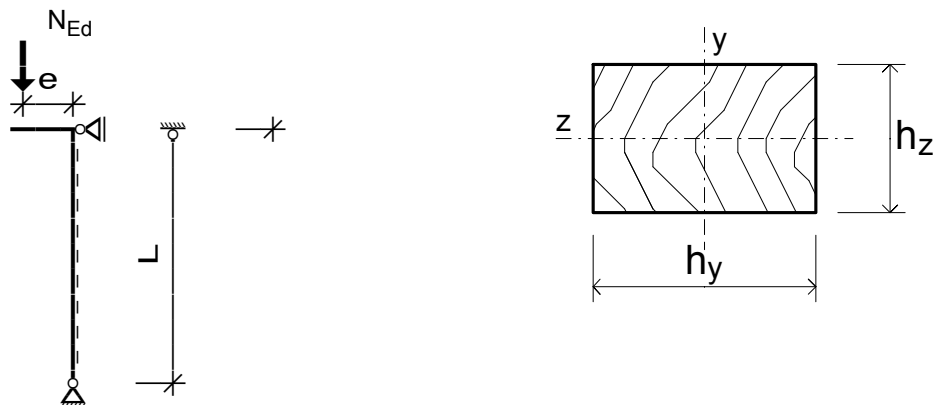
Depth $h =$	$\text{MIN}(h_y; h_z)$	= 100.00 mm
Radius of gyration $i =$	$\frac{h}{\sqrt{12}} = \frac{100.00}{\sqrt{12}}$	= 28.87 mm
Slenderness ratio $\lambda =$	$\frac{L}{i} = \frac{3500}{28.87}$	= 121.23
$\lambda_{rel} =$	$\frac{\lambda}{\pi} * \sqrt{\frac{f_{c,0,k}}{E_{0,0,05}}} = \frac{121.23}{3.14159} * \sqrt{\frac{21.00}{7400.00}}$	= 2.06
$\beta_c =$	$\text{IF}(T = \text{"Glulam"}; 0.1; 0.2)$	= 0.20
$k =$	$0.5 * (1 + \beta_c * (\lambda_{rel} - 0.3) + \lambda_{rel}^2)$	= 2.80
$k_c =$	$\frac{1}{k + \sqrt{k^2 - \lambda_{rel}^2}} = \frac{1}{2.80 + \sqrt{2.80^2 - 2.06^2}}$	= 0.213

#### Ultimate axial load capacity

$k_{c,fc,0,d} =$	$k_c * f_{c,0,d} = 0.213 * 12.92$	= 2.75 N/mm <sup>2</sup>
$N_{Ed,max} =$	$k_{c,fc,0,d} * h_y * h_z / 10^3 = 2.75 * 150.0 * 100.0 / 10^3$	= <b>41.25 kN</b>



### Axial load capacity of a timber post



#### Data given

Clear height $L =$	3.00 m
Depth $h_y =$	150.0 mm
Eccentricity $e_y =$	50.00 mm
Depth $h_z =$	100.0 mm
Eccentricity $e_z =$	0.00 mm

#### Loading

Vertical load $N_{Ed} =$	40.00 kN
Bending Moment $M_z = N_{Ed} * e_z = 40.00 * 0.00$	= 0.00 kNm
Bending Moment $M_y = N_{Ed} * e_y = 40.00 * 0.05$	= 2.00 kNm

#### Timber properties and parameters

Timber T	=	Softwood
Strength class $C_T$	=	C24
Service class $C_S$	=	2
Duration class $C_D$	=	medium-term
$E_{0,0,05}$	=	7400.00 N/mm <sup>2</sup>
Partial factor $\gamma_M =$		1.30
$f_{m,k}$	=	24.00 N/mm <sup>2</sup>
$f_{c,0,k}$	=	21.00 N/mm <sup>2</sup>
$k_{mod}$	=	0.80
Design compressive strength of timber:		
$f_{c,0,d} = k_{mod} * f_{c,0,k} / \gamma_M = 0.80 * 21.00 / 1.30$	=	12.92 N/mm <sup>2</sup>
Design bending strength of timber:		
Depth factor $k_h = \text{MAX}( 1.0 ; \text{MIN}( (150/h_y)^{0.2} ; 1.3 ) )$	=	1.000
$f_{m,y,d} = k_{mod} * k_h * f_{m,k} / \gamma_M = 0.80 * 1.000 * 24.00 / 1.30$	=	14.77 N/mm <sup>2</sup>
Depth factor $k_h = \text{MAX}( 1.0 ; \text{MIN}( (150/h_z)^{0.2} ; 1.3 ) )$	=	1.084
$f_{m,z,d} = k_{mod} * k_h * f_{m,k} / \gamma_M = 0.80 * 1.084 * 24.00 / 1.30$	=	16.01 N/mm <sup>2</sup>



### Design bending and compressive stresses

$$\text{Design compressive stress } \sigma_{c,0,d} = \frac{N_{Ed}}{h_y * h_z} = \frac{40000}{150.0 * 100.0} = 2.67 \text{ N/mm}^2$$

$$\text{Elastic section modulus } W_{yy} = \frac{h_z * h_y^2}{6} = \frac{100.0 * 150.0^2}{6} = 375.00 * 10^3 \text{ mm}^3$$

$$\text{Design bending stress } \sigma_{m,y,d} = \frac{M_y}{W_{yy}} = \frac{2000000}{375000} = 5.33 \text{ N/mm}^2$$

$$\text{Elastic section modulus } W_{zz} = \frac{h_z^2 * h_y}{6} = \frac{100.0^2 * 150.0}{6} = 250.00 * 10^3 \text{ mm}^3$$

$$\text{Design bending stress } \sigma_{m,z,d} = \frac{M_z}{W_{zz}} = \frac{0.00}{250000} = 0.00 \text{ N/mm}^2$$

### Calculations for buckling about z-z axis

$$\text{Radius of gyration } i = \frac{h_z}{\sqrt{12}} = \frac{100.0}{\sqrt{12}} = 28.87 \text{ mm}$$

$$\text{Slenderness ratio } \lambda = \frac{L}{i} = \frac{3000}{28.87} = 103.91$$

$$\lambda_{rel} = \frac{\lambda}{\pi} * \sqrt{\frac{f_{c,0,k}}{E_{0,0,05}}} = \frac{103.91}{3.14159} * \sqrt{\frac{21.00}{7400.00}} = 1.76$$

$$\beta_c = \text{IF}(T = \text{"Glulam"}; 0.1; 0.2) = 0.20$$

$$k = \frac{0.5 * (1 + \beta_c * (\lambda_{rel} - 0.3) + \lambda_{rel}^2)}{1} = \frac{1}{1} = 2.19$$

$$k_c = \frac{1}{k + \sqrt{k^2 - \lambda_{rel}^2}} = \frac{1}{2.19 + \sqrt{2.19^2 - 1.76^2}} = 0.286$$

$$\frac{\sigma_{c,0,d}}{k_c * f_{c,0,d}} + 0.7 * \frac{\sigma_{m,y,d}}{f_{m,y,d}} + \frac{\sigma_{m,z,d}}{f_{m,z,d}} = \frac{2.67}{0.286 * 12.92} + 0.7 * \frac{5.33}{14.77} + \frac{0.00}{16.01} = 0.98 \leq 1$$

### Calculations for buckling about y-y axis

$$\text{Radius of gyration } i = \frac{h_y}{\sqrt{12}} = \frac{150.0}{\sqrt{12}} = 43.30 \text{ mm}$$

$$\text{Slenderness ratio } \lambda = \frac{L}{i} = \frac{3000}{43.30} = 69.28$$

$$\lambda_{rel} = \frac{\lambda}{\pi} * \sqrt{\frac{f_{c,0,k}}{E_{0,0,05}}} = \frac{69.28}{3.14159} * \sqrt{\frac{21.00}{7400.00}} = 1.17$$

$$k = \frac{0.5 * (1 + \beta_c * (\lambda_{rel} - 0.3) + \lambda_{rel}^2)}{1} = \frac{1}{1} = 1.27$$

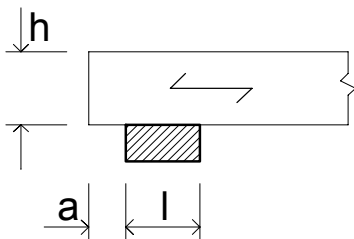
$$k_c = \frac{1}{k + \sqrt{k^2 - \lambda_{rel}^2}} = \frac{1}{1.27 + \sqrt{1.27^2 - 1.17^2}} = 0.567$$

$$\frac{\sigma_{c,0,d}}{k_c * f_{c,0,d}} + \frac{\sigma_{m,y,d}}{f_{m,y,d}} + 0.7 * \frac{\sigma_{m,z,d}}{f_{m,z,d}} = \frac{2.67}{0.567 * 12.92} + \frac{5.33}{14.77} + 0.7 * \frac{0.00}{16.01} = 0.73 \leq 1$$



## Chapter 3: Supports

### Compression perpendicular to the grain at end bearing



#### Data given

Width b =	100.0 mm
Depth h =	150.0 mm
Support l =	100.0 mm

#### Material properties:

Timber T	= Softwood
Strength class C <sub>T</sub>	= C24
Bearing strength f <sub>c,90,k</sub>	= 2.50 N/mm <sup>2</sup>
Service class C <sub>S</sub>	= 2
Duration class C <sub>D</sub>	= medium-term
Partial factor γ <sub>M</sub>	= 1.30

f <sub>m,k</sub>	= 24.00 N/mm <sup>2</sup>
k <sub>mod</sub>	= 0.80
f <sub>c,90,d</sub> = k <sub>mod</sub> * $\frac{f_{c,90,k}}{\gamma_M}$	= 0.80 * $\frac{2.50}{1.30}$
	= 1.54 N/mm <sup>2</sup>

#### At end bearing

$$\frac{h}{3} = \frac{150.0}{3} = 50.0 > a$$

$$k_{c,90} = \text{MAX}(1; \text{MIN}\left(\left(2.38 - \frac{l}{250}\right) * \left(1 + \frac{h}{12 * l}\right); 4\right)) = 2.23$$

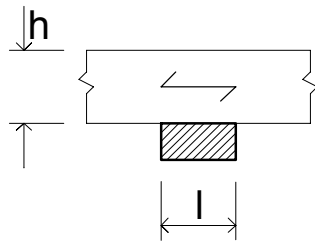
$$\sigma_{c,90,d} = k_{c,90} * f_{c,90,d} = 2.23 * 1.54 = 3.43 \text{ N/mm}^2$$

#### Ultimate capacity of bearing at ULS

$$F_{\text{MAX}} = \sigma_{c,90,d} * b * l = 3.43 * 10.0 * 10.0 = 34.3 \text{ kN}$$



### Compression perpendicular to the grain at internal bearing



#### Data given

Width b =	100.0 mm
Depth h =	200.0 mm
Support l =	100.0 mm

#### Material properties:

Timber T	= Softwood
Strength class C <sub>T</sub>	= C24
Bearing strength f <sub>c,90,k</sub>	= 2.50 N/mm <sup>2</sup>
Service class C <sub>S</sub>	= 2
Duration class C <sub>D</sub>	= medium-term
Partial factor γ <sub>M</sub>	= 1.30

$$f_{m,k} = 24.00 \text{ N/mm}^2$$

$$k_{\text{mod}} = 0.80$$

$$f_{c,90,d} = k_{\text{mod}} \cdot \frac{f_{c,90,k}}{\gamma_M} = 0.80 \cdot \frac{2.50}{1.30} = 1.54 \text{ N/mm}^2$$

#### At internal bearing

$$k_{c,90} = \text{MAX}(1; \text{MIN}\left(\left(2.38 - \frac{l}{250}\right) \cdot \left(1 + \frac{h}{6 \cdot l}\right); 4\right)) = 2.64$$

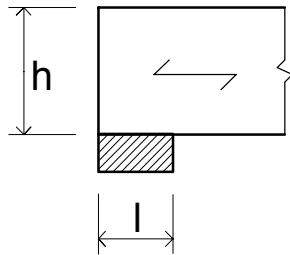
$$\sigma_{c,90,d} = k_{c,90} \cdot f_{c,90,d} = 2.64 \cdot 1.54 = 4.07 \text{ N/mm}^2$$

#### Ultimate capacity of bearing at ULS

$$F_{\text{MAX}} = \sigma_{c,90,d} \cdot b \cdot l = 4.07 \cdot 10.0 \cdot 10.0 = 40.7 \text{ kN}$$



### Shear capacity at a support



#### Data given

Width  $b = 100.0$  mm  
Depth  $h = 150.0$  mm  
Support  $l = 100.0$  mm

#### Material properties:

Timber  $T =$  Softwood  
Strength class  $C_T =$  C24  
Shear strength  $f_{v,k} = 2.50$  N/mm<sup>2</sup>  
Service class  $C_S = 2$   
Duration class  $C_D =$  medium-term  
Partial factor  $\gamma_M = 1.30$

$k_{mod} = 0.80$

$f_{v,d} = k_{mod} \cdot \frac{f_{v,k}}{\gamma_M} = 0.80 \cdot \frac{2.50}{1.30} = 1.54$  N/mm<sup>2</sup>

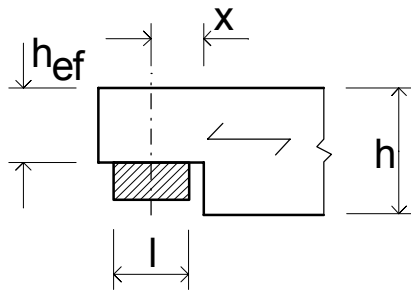
#### Shear capacity

$V_{max} = \frac{f_{v,d} \cdot b \cdot h}{1.5} = \frac{0.154 \cdot 100.0 \cdot 150.0}{1.5} = 15.40$  kN





### Shear capacity at a support notched at the bottom



#### Data given

Width b =	100.0 mm
Depth h =	200.0 mm
Depth h <sub>ef</sub> =	120.0 mm
Distance x =	75.0 mm
Support l =	100.0 mm

#### Material properties:

Timber T	= Softwood
Strength class C <sub>T</sub>	= C24
Shear strength f <sub>v,k</sub>	= 2.50 N/mm <sup>2</sup>
Service class C <sub>S</sub>	= 2
Duration class C <sub>D</sub>	= medium-term

Partial factor  $\gamma_M = 1.30$

$k_{mod} = 0.80$

$f_{v,d} = k_{mod} \cdot \frac{f_{v,k}}{\gamma_M} = 0.80 \cdot \frac{2.50}{1.30} = 1.54 \text{ N/mm}^2$

#### Shear capacity

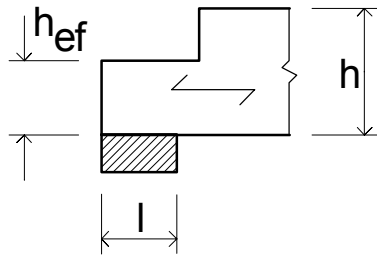
$\alpha = \frac{h_{ef}}{h} = \frac{120.0}{200.0} = 0.60$

$k_v = \text{MIN}\left(\frac{5}{\sqrt{h} \cdot \left(\sqrt{\alpha \cdot (1-\alpha)} + 0.8 \cdot \frac{x}{h} \cdot \sqrt{\frac{1-\alpha^2}{\alpha}}\right)}; 1\right) = 0.425$

$V_{max} = \frac{k_v \cdot f_{v,d} \cdot b \cdot h_{ef}}{1.5} = \frac{0.425 \cdot 1.54 \cdot 10.0 \cdot 12.0}{1.5} = 5.24 \text{ kN}$



### Shear capacity at a support notched at the top



#### Data given

Width  $b = 100.0$  mm  
Depth  $h_{ef} = 120.0$  mm  
Support  $l = 100.0$  mm

#### Material properties:

Timber  $T =$  Softwood  
Strength class  $C_T =$  C24  
Shear strength  $f_{v,k} = 2.50$  N/mm<sup>2</sup>  
Service class  $C_S = 2$   
Duration class  $C_D =$  medium-term  
Partial factor  $\gamma_M = 1.30$

$k_{mod} = 0.80$

$f_{v,d} = k_{mod} \cdot \frac{f_{v,k}}{\gamma_M} = 0.80 \cdot \frac{2.50}{1.30} = 1.54$  N/mm<sup>2</sup>

#### Shear capacity

$V_{max} = \frac{f_{v,d} \cdot b \cdot h_{ef}}{1.5} = \frac{0.154 \cdot 10.0 \cdot 12.0}{1.5} = 12.32$  kN